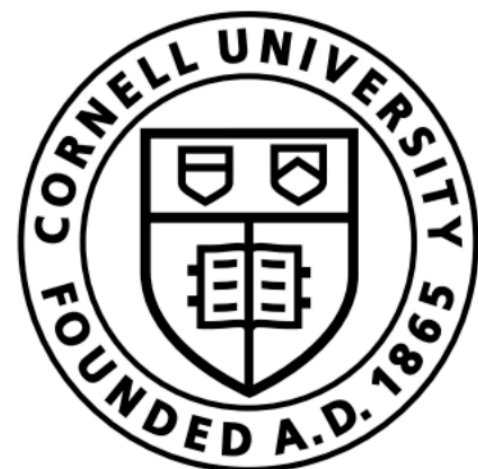


Policy-Gradient Training of Language Models for Ranking

Ge Gao, Jonathan D. Chang, Claire Cardie, Kianté Brantley, Thorsten Joachims



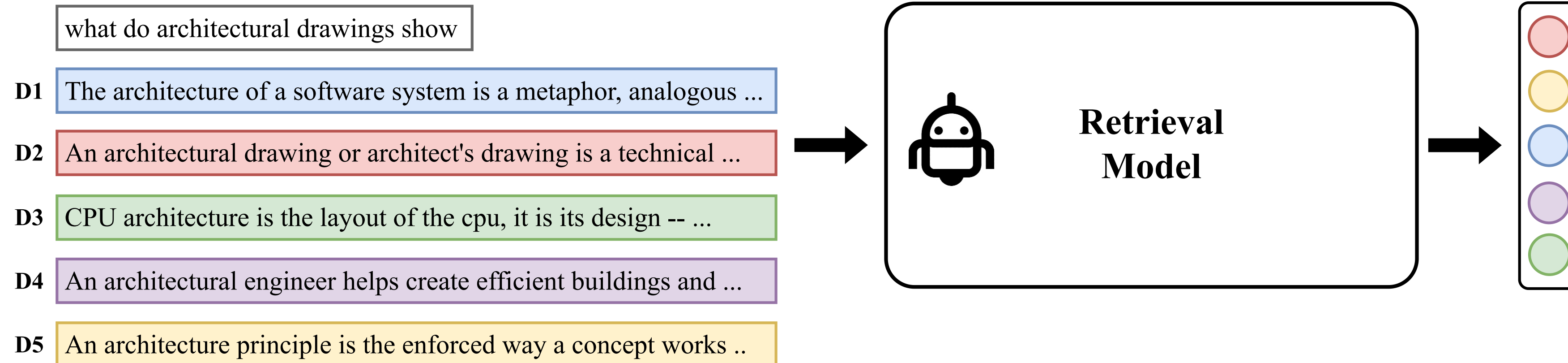
Cornell Bowers CIS
Computer Science

**CORNELL
TECH**

Background

- Task definition of retrieval: rank documents based on their relevance to a query

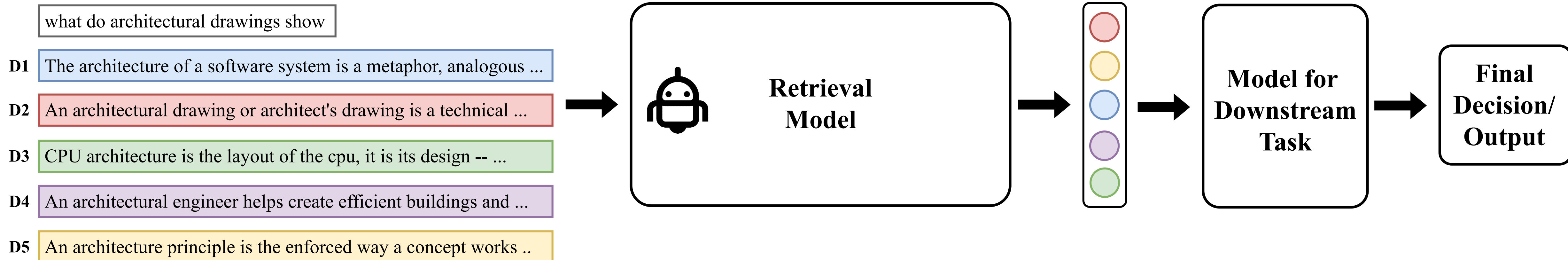
Query and Documents



Background

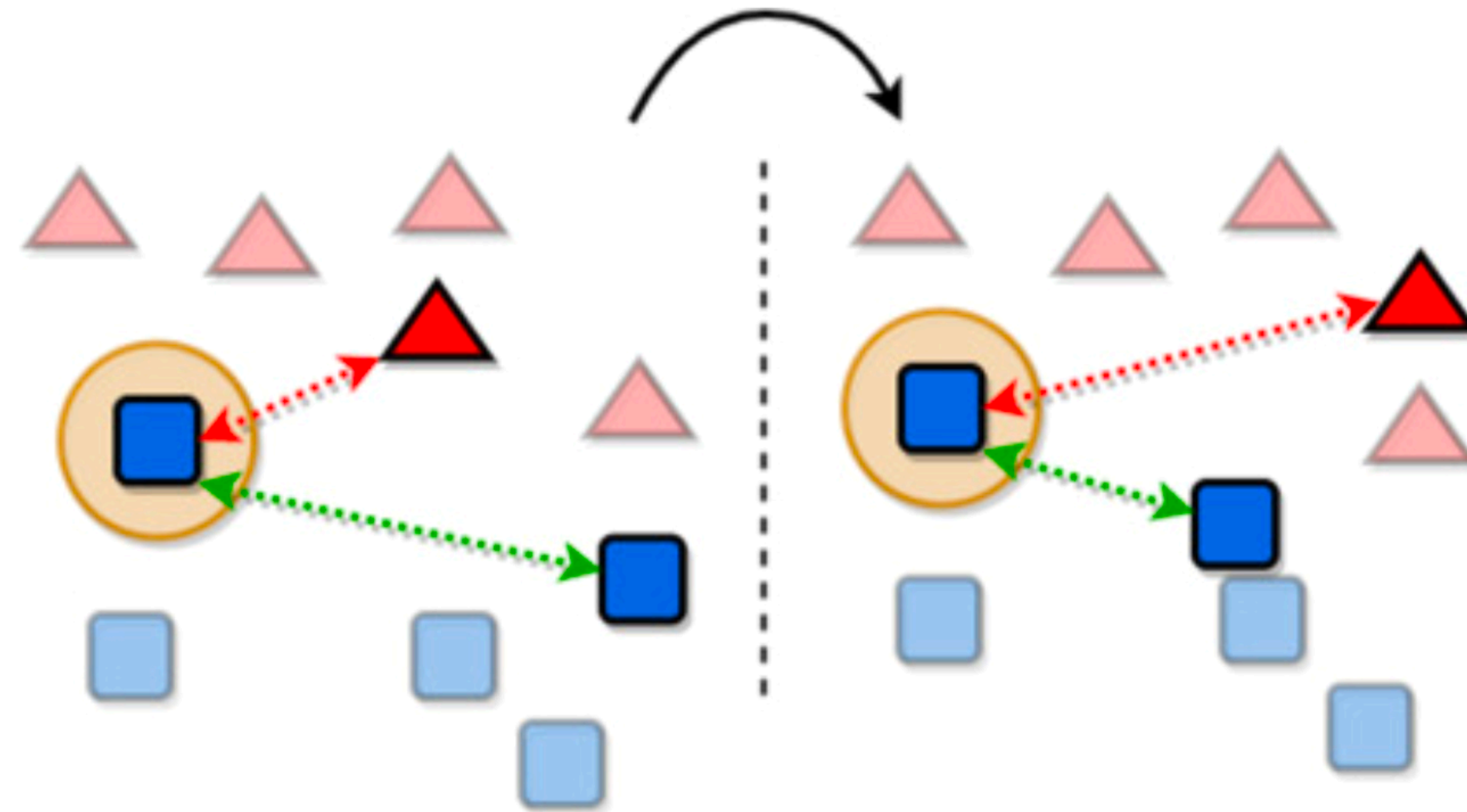
- Task definition of retrieval: rank documents based on their relevance to a query
- Application of retrieval models: ranked documents are input to some downstream models; separate from training retrieval models

Query and Documents



Background

- Conventional training objectives: contrastive loss, requiring ground truth annotation for relevant documents and estimation for truly irrelevant documents (i.e. hard negatives)



Overview

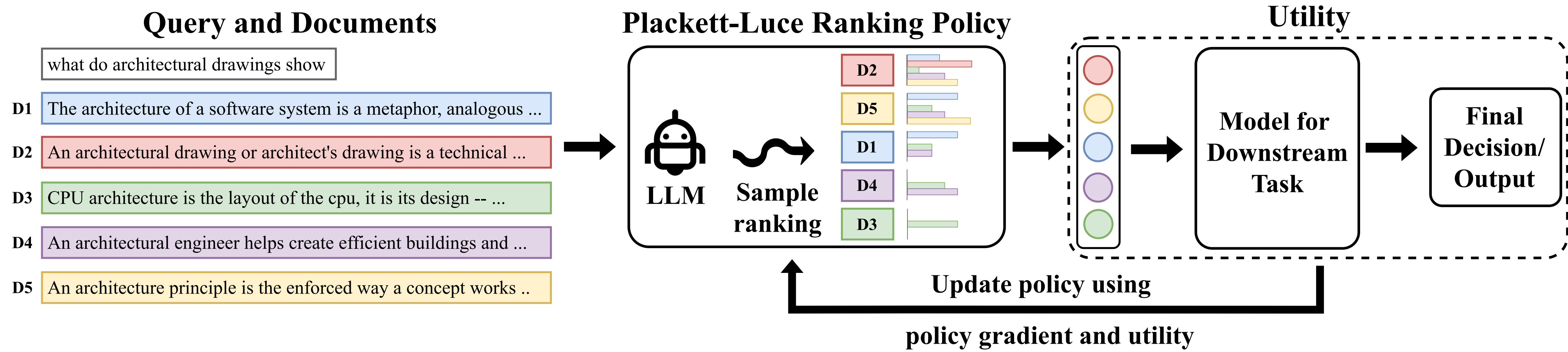
- We introduce **Neural PG-RANK** to train LLM-based retrieval models that directly optimize downstream decision-making quality

Overview

- We introduce **Neural PG-RANK** to train LLM-based retrieval models that directly optimize downstream decision-making quality
 - Learns to rank by instantiating a LLM as a Plackett-Luce ranking policy
 - End-to-end training of retrieval models as part of larger pipelines via policy gradient
 - Can optimize the ranker for any cardinal loss function evaluating the downstream decisions

Overview

- We introduce **Neural PG-RANK** to train LLM-based retrieval models that directly optimize downstream decision-making quality



Setting

- Define the utility of a ranking policy for a given query

$$U(\pi|q) = \mathbb{E}_{r \sim \pi(\cdot|q)} [\Delta(r|q)]$$

Utility function

Ranking

Query

Setting

- Define the utility of a ranking policy for a given query

$$U(\pi|q) = \mathbb{E}_{r \sim \pi(\cdot|q)} [\Delta(r|q)]$$

Utility function

Query
Ranking

- Learning objective is to learn a ranking policy that optimizes the expected utility over the query distribution

$$\pi^* = \operatorname{argmax}_{\pi \in \Pi} \mathbb{E}_{q \sim \mathcal{Q}} [U(\pi|q)]$$

Method

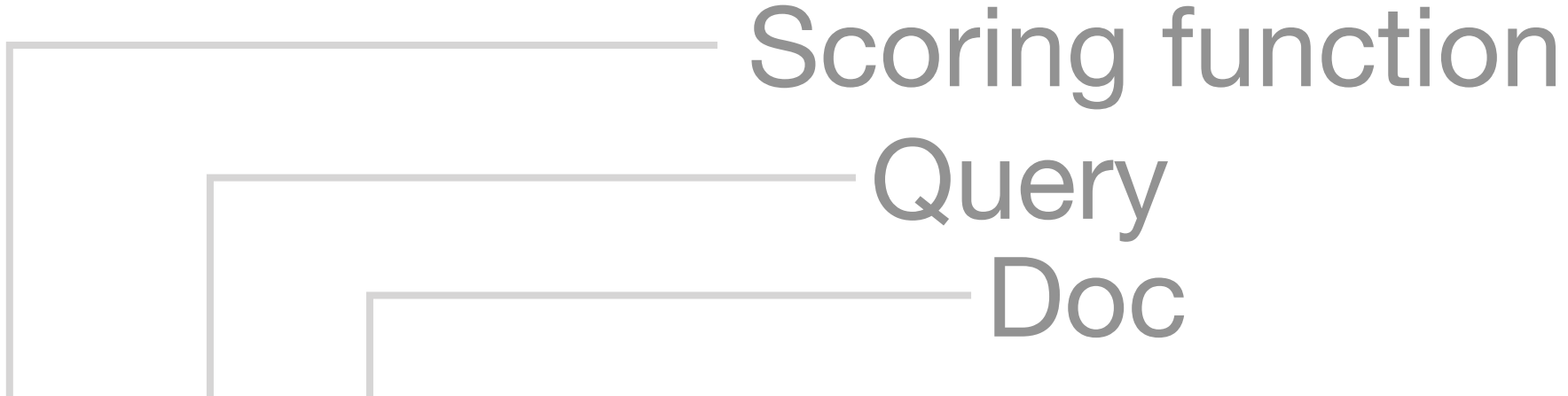
- Define a Plackett-Luce ranking policy

Definition 1 (Plackett-Luce Model (Plackett, 1975; Luce, 1959)). *Given the utility scores of the N items, $\mathbf{w} = [w_1, w_2, \dots, w_N]^T$, the probability of observing a certain ordered list of these items, (i_1, i_2, \dots, i_N) , is defined as*

$$p((i_1, i_2, \dots, i_N); \mathbf{w}) = \prod_{j=1}^N \frac{\exp(w_{i_j})}{\sum_{l=j}^N \exp(w_{i_l})}. \quad (1)$$

Method

- Define a Plackett-Luce ranking policy
 - expressed as a product of softmax distributions
 - based on query-document relevance scores


$$\pi_{\theta}(r|q) = \prod_{i=1}^n \frac{\exp s_{\theta}(q, d_{r(i)})}{\sum_{j \in \{r(i), \dots, r(n)\}} \exp s_{\theta}(q, d_j)}$$

Method

- We use REINFORCE

$$\begin{aligned}\nabla_{\theta} U(\pi_{\theta}|q) &= \nabla_{\theta} \mathbb{E}_{r \sim \pi_{\theta}(\cdot|q)} [\Delta(r|q)] \\ &= \mathbb{E}_{r \sim \pi_{\theta}(\cdot|q)} [\nabla_{\theta} \log \pi_{\theta}(r|q) \Delta(r|q)]\end{aligned}$$

Method

- We use REINFORCE
 - + Monte Carlo sampling with N samples
 - + Variance reduction with leave-one-out baseline

$$\hat{\nabla}_{\theta} U(\pi_{\theta}|q) = \frac{1}{N} \sum_i \left[\nabla_{\theta} \log \pi_{\theta}(r_i|q) \left(\Delta(r_i|q) - \frac{1}{N-1} \sum_{j \neq i} \Delta(r_j|q) \right) \right]$$

Method

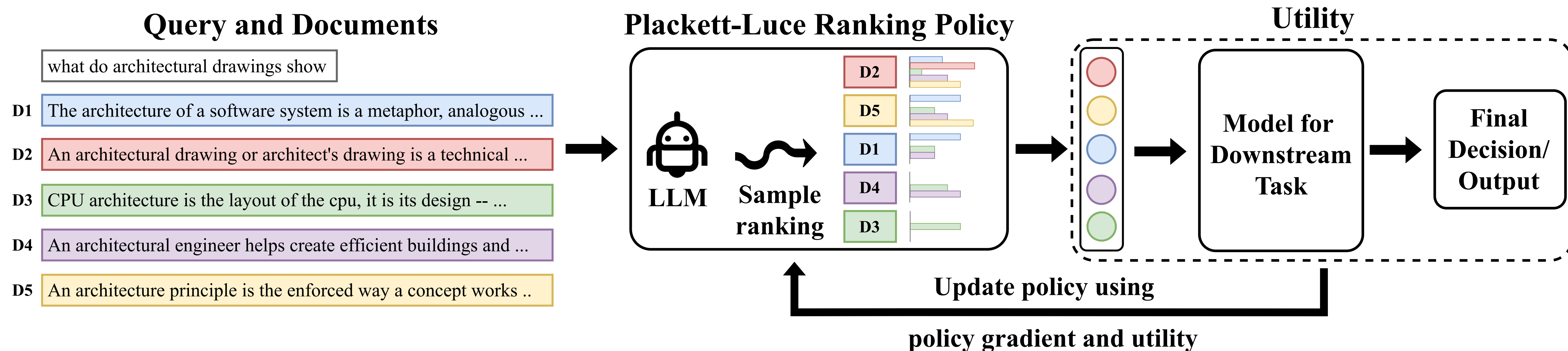
- We use REINFORCE
 - + Monte Carlo sampling with N samples
 - + Variance reduction with leave-one-out baseline
 - + nDCG@10 as utility function

$$\begin{aligned}\hat{\nabla}_{\theta} U(\pi_{\theta}|q) &= \frac{1}{N} \sum_i \left[\nabla_{\theta} \log \pi_{\theta}(r_i|q) \left(\Delta(r_i|q) - \frac{1}{N-1} \sum_{j \neq i} \Delta(r_j|q) \right) \right] \\ &= \frac{1}{N} \sum_i \left[\sum_k \nabla_{\theta} \log \pi_{\theta}(r_{i,k}|q, r_{i,1:k-1}) \right. \\ &\quad \left. \left(\text{nDCG}(r_{i,k:}|q, r_{i,1:k-1}) - \frac{1}{N-1} \sum_{j \neq i} \text{nDCG}(r_{j,k:}|q, r_{i,1:k-1}) \right) \right]\end{aligned}$$

Utility score for the partial ranking til k

Utility

- nDCG@10: score between 0 and 1; higher means better ranking
- nDCG@10 is an approximation of the downstream utility in our work
- Assumption: higher nDCG@10 relates to better downstream task performance



Experimental Setup

- Data: MS MARCO for training; BEIR [Thakur et al., 2021] for evaluation

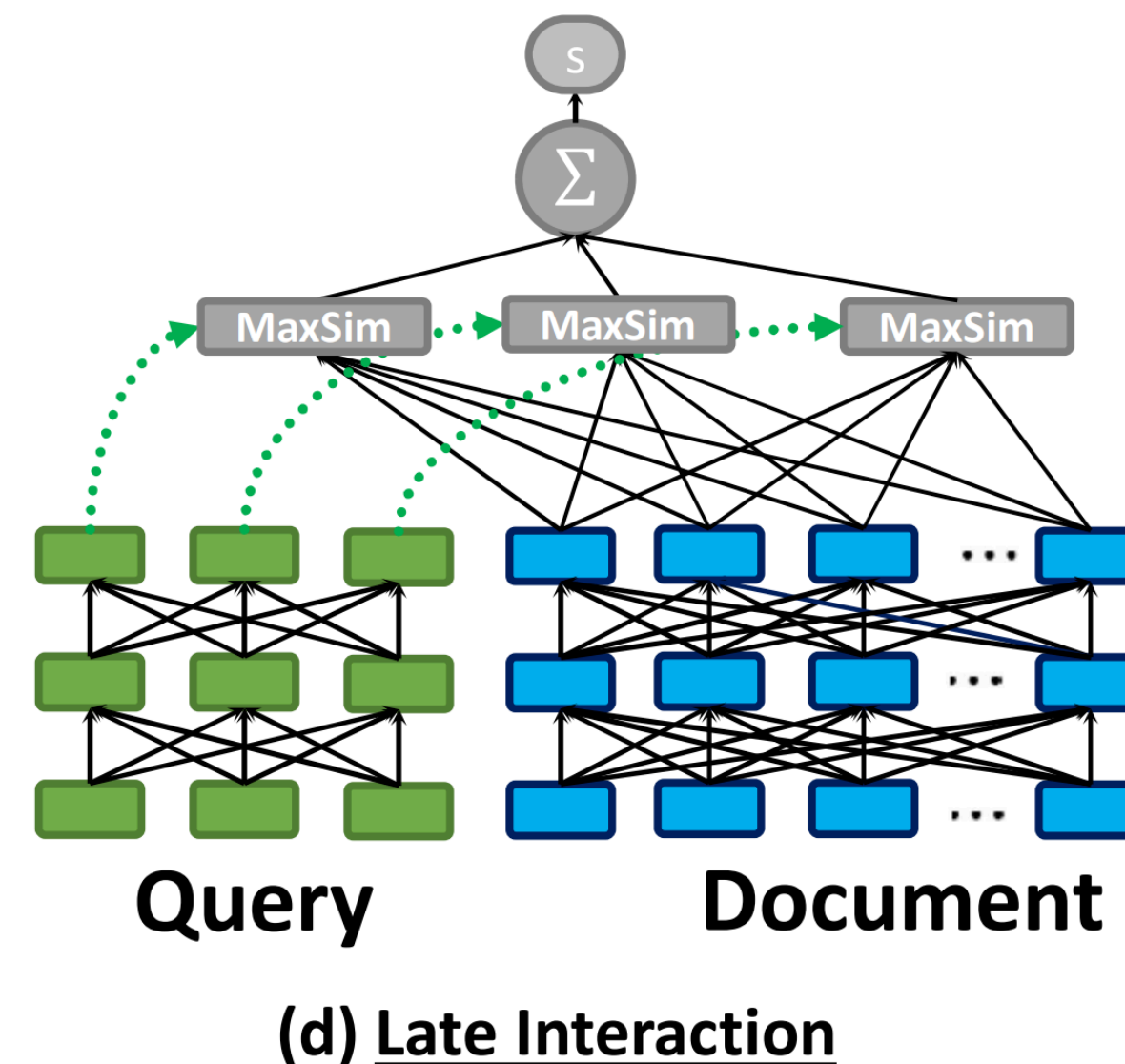
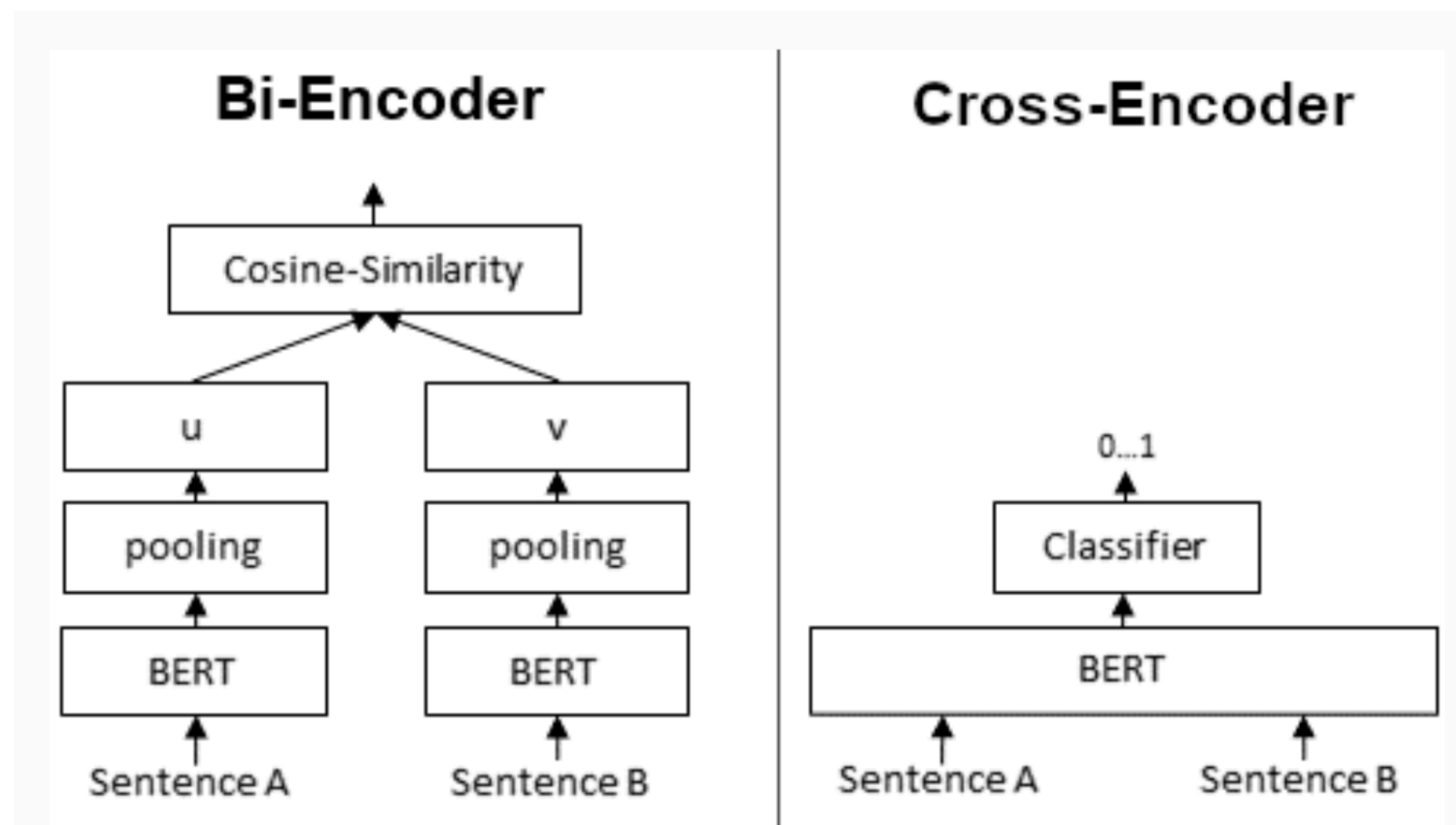
| Split (→) | | | | | Train | Dev | Test | | | Avg. Word Lengths | |
|--|-------------|---------------------|-------|-----------|---------|--------|--------|------------|------------|-------------------|----------|
| Task (↓) | Domain (↓) | Dataset (↓) | Title | Relevancy | #Pairs | #Query | #Query | #Corpus | Avg. D / Q | Query | Document |
| Passage-Retrieval | Misc. | MS MARCO [45] | ✗ | Binary | 532,761 | — | 6,980 | 8,841,823 | 1.1 | 5.96 | 55.98 |
| Bio-Medical Information Retrieval (IR) | Bio-Medical | TREC-COVID [65] | ✓ | 3-level | — | — | 50 | 171,332 | 493.5 | 10.60 | 160.77 |
| | Bio-Medical | NFCorpus [7] | ✓ | 3-level | 110,575 | 324 | 323 | 3,633 | 38.2 | 3.30 | 232.26 |
| | Bio-Medical | BioASQ [61] | ✓ | Binary | 32,916 | — | 500 | 14,914,602 | 4.7 | 8.05 | 202.61 |
| Question Answering (QA) | Wikipedia | NQ [34] | ✓ | Binary | 132,803 | — | 3,452 | 2,681,468 | 1.2 | 9.16 | 78.88 |
| | Wikipedia | HotpotQA [76] | ✓ | Binary | 170,000 | 5,447 | 7,405 | 5,233,329 | 2.0 | 17.61 | 46.30 |
| | Finance | FiQA-2018 [44] | ✗ | Binary | 14,166 | 500 | 648 | 57,638 | 2.6 | 10.77 | 132.32 |
| Tweet-Retrieval | Twitter | Signal-1M (RT) [59] | ✗ | 3-level | — | — | 97 | 2,866,316 | 19.6 | 9.30 | 13.93 |
| News Retrieval | News | TREC-NEWS [58] | ✓ | 5-level | — | — | 57 | 594,977 | 19.6 | 11.14 | 634.79 |
| | News | Robust04 [64] | ✗ | 3-level | — | — | 249 | 528,155 | 69.9 | 15.27 | 466.40 |
| Argument Retrieval | Misc. | ArguAna [67] | ✓ | Binary | — | — | 1,406 | 8,674 | 1.0 | 192.98 | 166.80 |
| | Misc. | Touché-2020 [6] | ✓ | 3-level | — | — | 49 | 382,545 | 19.0 | 6.55 | 292.37 |
| Duplicate-Question Retrieval | StackEx. | CQADupStack [25] | ✓ | Binary | — | — | 13,145 | 457,199 | 1.4 | 8.59 | 129.09 |
| | Quora | Quora | ✗ | Binary | — | 5,000 | 10,000 | 522,931 | 1.6 | 9.53 | 11.44 |
| Entity-Retrieval | Wikipedia | DBPedia [21] | ✓ | 3-level | — | 67 | 400 | 4,635,922 | 38.2 | 5.39 | 49.68 |
| Citation-Prediction | Scientific | SCIDOCS [9] | ✓ | Binary | — | — | 1,000 | 25,657 | 4.9 | 9.38 | 176.19 |
| Fact Checking | Wikipedia | FEVER [60] | ✓ | Binary | 140,085 | 6,666 | 6,666 | 5,416,568 | 1.2 | 8.13 | 84.76 |
| | Wikipedia | Climate-FEVER [14] | ✓ | Binary | — | — | 1,535 | 5,416,593 | 3.0 | 20.13 | 84.76 |
| | Scientific | SciFact [68] | ✓ | Binary | 920 | — | 300 | 5,183 | 1.1 | 12.37 | 213.63 |

Experimental Setup

- Data: MS MARCO for training; BEIR [Thakur et al., 2021] for evaluation
- Evaluation metric: nDCG@10
- Our ranking policy: either SBERT [Reimers & Gurevych, 2019] or TAS-B [Hofstätter et al., 2021] as warmstart, with Neural PG-RANK method as fine-tuning

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- Comparison systems: supervised learning SOTA bi-encoder models

| Method | Source of Negative Docs | | | Additional Supervision | Loss |
|----------------------------------|-------------------------|------|-------------|------------------------|--------------------------|
| | In-Batch | BM25 | Dense Model | | |
| SBERT (Reimers & Gurevych, 2019) | | ✓ | ✓✓✓ | ✓ | MarginMSE + NLL |
| TAS-B (Hofstätter et al., 2021) | ✓ | ✓ | | ✓✓ | MarginMSE + Distillation |
| SPLADEv2 (Formal et al., 2021) | | ✓ | ✓✓ | ✓ | MarginMSE + Sparsity |
| Neural PG-RANK (Ours) | | | ✓ | | Utility Maximization |

Result: Second-Stage Reranking

- Setup: search over a candidate set of 1k documents per query

Result: Second-Stage Reranking

- Setup: search over a candidate set of 1k documents per query
- In-domain results:
 - Performance gains with both warmstart models (nDCG@10)

| Dataset | Domain | Comparison Systems | | | Ours: Neural PG-RANK | |
|--------------|--------|--------------------|--------|-----------|----------------------|--------------|
| | | SBERT* | TAS-B* | SPLADEv2* | with SBERT | with TAS-B |
| MS MARCO dev | misc. | 0.892 | 0.893 | 0.900 | 0.987 | <u>0.982</u> |

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| MS MARCO dev | misc. | 0.892 | 0.893 | 0.900 | 0.987 | <u>0.982</u> |

- More gains in terms of nDCG@k with smaller k (nDCG@1 below)

| Dataset | Comparison Systems | | | Ours: Neural PG-RANK | |
|---------------------------|--------------------|--------|-----------|----------------------|--------------|
| | SBERT* | TAS-B* | SPLADEv2* | with SBERT | with TAS-B |
| MS MARCO dev [‡] | 0.826 | 0.819 | 0.830 | 0.975 | <u>0.965</u> |

Result: Second-Stage Reranking

- Out-of-domain results:

| Dataset | Domain | Comparison Systems | | | Ours: Neural PG-RANK | |
|---------------|-------------|--------------------|--------------|--------------|----------------------|--------------|
| | | SBERT* | TAS-B* | SPLADEv2* | with SBERT | with TAS-B |
| MS MARCO dev | misc. | 0.892 | 0.893 | 0.900 | 0.987 | <u>0.982</u> |
| TREC-DL 2019 | misc. | <u>0.743</u> | 0.749 | 0.749 | 0.742 | 0.741 |
| TREC-COVID | bio-medical | 0.764 | 0.711 | <u>0.731</u> | 0.690 | 0.630 |
| NFCorpus | bio-medical | <u>0.308</u> | 0.320 | 0.341 | 0.249 | 0.303 |
| NQ | Wikipedia | 0.836 | 0.836 | 0.854 | <u>0.869</u> | 0.878 |
| HotpotQA | Wikipedia | 0.747 | 0.785 | 0.834 | 0.902 | <u>0.900</u> |
| FiQA-2018 | finance | <u>0.291</u> | 0.279 | 0.342 | 0.131 | 0.139 |
| ArguAna | misc. | 0.351 | 0.479 | 0.480 | <u>0.354</u> | 0.443 |
| Touché-2020 | misc. | 0.480 | 0.423 | <u>0.460</u> | 0.363 | 0.361 |
| Quora | Quora | 0.962 | 0.982 | <u>0.967</u> | 0.963 | 0.982 |
| DBPedia | Wikipedia | 0.513 | 0.513 | 0.533 | 0.521 | <u>0.525</u> |
| SCIDOCS | scientific | 0.144 | <u>0.151</u> | 0.163 | 0.108 | 0.136 |
| FEVER | Wikipedia | 0.931 | 0.911 | <u>0.929</u> | 0.907 | <u>0.913</u> |
| Climate-FEVER | Wikipedia | <u>0.442</u> | 0.433 | 0.444 | 0.438 | 0.383 |
| SciFact | scientific | <u>0.597</u> | 0.579 | 0.696 | 0.316 | 0.410 |

Result: Second-Stage Reranking

- Out-of-domain results:

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Result: Second-Stage Reranking

- Out-of-domain results:

| Dataset | Domain | Comparison Systems | | | Ours: Neural PG-RANK | |
|---------------|-------------|--------------------|--------------|--------------|----------------------|--------------|
| | | SBERT* | TAS-B* | SPLADEv2* | with SBERT | with TAS-B |
| MS MARCO dev | misc. | 0.892 | 0.893 | 0.900 | 0.987 | <u>0.982</u> |
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Result: Second-Stage Reranking

- Setup: search over a candidate set of 1k documents per query
- In-domain results:
 - Performance gains with both warmstart models
 - More gains in terms of nDCG@k with smaller k (nDCG@1, 3, 5)
- Out-of-domain results:
 - Comparable generalization to in-domain results
 - Notable improvements on widely-studied QA datasets
 - Weaker in the domain of bio-medicine, science and finance

Result: First-Stage Retrieval

- Setup: search over all documents per query

Result: First-Stage Retrieval

- Setup: search over all documents per query
- In-domain results:
 - Suboptimal compared to warmstart models

| Dataset | Comparison Systems | | | | Ours: Neural PG-RANK | |
|--------------|--------------------|--------------|--------|--------------|----------------------|------------|
| | BM25 | SBERT* | TAS-B* | SPLADEv2* | with SBERT | with TAS-B |
| MS MARCO dev | 0.228 | 0.434 | 0.407 | <u>0.433</u> | 0.416 | 0.401 |

Summary

- We introduce **Neural PG-RANK** to train LLM-based retrieval models that directly optimize downstream decision-making quality
 - Learns to rank by instantiating a LLM as a Plackett-Luce ranking policy
 - End-to-end training of retrieval models as part of larger pipelines via policy gradient
 - Can optimize the ranker for any cardinal loss function evaluating the downstream decisions
- When the training objective aligns with the evaluation setup, Neural PG-RANK yields remarkable in-domain performance improvement, with substantial out-of-domain generalization to some critical datasets employed in downstream QA tasks.